

## Detection of seepages in flood embankments using the ElasticNET method

**Abstract.** The presented article discusses the proposition of using an algorithm based on the ElasticNET method to obtain accurate and reproducible results of reconstruction of tomographic images. In particular, the research concerned solving of the inverse problem in electrical tomography with reference to levees and dams. To enable the reconstruction of high resolution images using the impedance tomography, the ElasticNET algorithm was used, which is a combination of two methods: dorsal regression and LASSO. The results of the research have shown that thanks to the ElasticNET method you can obtain high resolution images that are faithful representation of the cross-section of the dam.

**Streszczenie.** W zaprezentowanym artykule omówiono propozycję użycia algorytmu opartego na metodzie Elastic net w celu uzyskania dokładnych i powtarzalnych wyników rekonstrukcji obrazów tomograficznych. W szczególności badania dotyczyły rozwiązywania problemu odwrotnego w tomografii elektrycznej w odniesieniu do wałów przeciwpowodziowych i zapór. Aby umożliwić rekonstrukcję obrazów o wysokiej rozdzielczości stosując tomografię impedancyjną zastosowano algorytm ElasticNET, który jest połączeniem dwóch metod: regresji grzbietowej i LASSO. Wyniki badań wykazały, że dzięki metodzie ElasticNET można uzyskać obrazy o wysokiej rozdzielczości, będące wiernym odwzorowaniem przekroju zapory wodnej. (**Wykrywanie przecieków w wałach przeciwpowodziowych przy użyciu metody ElasticNET.**)

**Keywords:** electrical impedance tomography, elastic net, inverse problem.

**Słowa kluczowe:** elektryczna tomografia impedancyjna, elastic net, problem odwrotny..

### Introduction

Electric tomography is based on the transformation of data taken from the surface of the tested object into the image of its cross-section. There are many methods to optimize the obtained image by solving the appropriate objective function [1-5,13,15,16,20-25,32]. The algorithm based on the ElasticNET presented in this article is a new proposal in tomography.

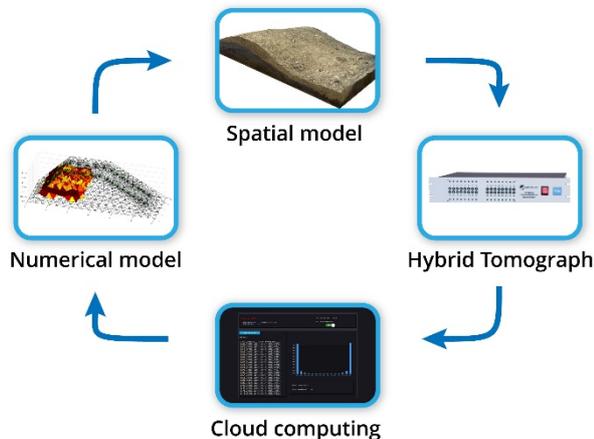


Fig. 1. Model of measurement system.

The way of working of electrical impedance tomography (EIT) consists in introducing electrical voltage to the tested object by means of a set of electrodes located on the surface of the object. Next, the measured values of electrical potentials between individual electrode pairs are collected. Conductance of individual sections of the cross-section of the tested object is reconstructed on the basis of known values of voltages and measured values of potentials. Reconstruction of the image obtained by electrical tomography requires sophisticated modeling. This method of imaging consists in the fact that the conductivity distribution of the tested object is estimated on the basis of measurements of electrical voltages and electrode potentials on the surface of their contact with the tested

object. In order to obtain quantitative data on changes in the conductivity inside an object, it is more effective to apply a non-linear model in differential imaging [1,6-12,14,17-19,26-31]. In Fig. 1 shows the model of the measurement system.

### ElasticNET

Let's consider the problem of recognizing linear dependencies

$$(1) \quad Y = X\beta + \varepsilon$$

where  $Y \in R^n$ ,  $X \in R^{n \times (k+1)}$  are the observation matrices of a output variable and predictive variables respectively,  $\beta \in R^{k+1}$  means a matrix of structural parameters, while  $\varepsilon \in R^n$  vector of independent random variables. The well-known method of least squares consists in estimating unknown parameters  $\beta = (\beta_0, \beta_1, \dots, \beta_k)$  listed in the equation (1) by solving the task (2).

$$(2) \quad \min_{\beta \in R^{k+1}} \|Y - X\beta\|^2$$

If  $\det(X^T X) \neq 0$ , then the best estimator of unknown parameters  $\beta$  equals  $\hat{\beta} = (X^T X)^{-1} X^T Y$ .

In case the independent (input) variables are strongly correlated (collinear) to each other, the matrix  $X^T X$  approaching a singular matrix. Using KMNK, the large absolute values of estimates (estimators) for unknown parameters are obtained. The predictions generated by such models are quite unstable. In tomography, the main goal is reconstruction of the image on the basis of the obtained from the electrodes measurements. During making measurements, we can see that the obtained values are highly correlated. Hence, we face the problem of input variables collinearity in the model (1). The possible solution is the introduction of an additional penalty. The penalty factor depending on the size of the parameter estimations in the task (2) consents the estimators to shrink. Finally, let's consider the task (3).

$$(3) \quad \min_{(\beta_0, \beta') \in \mathbb{R}^{k+1}} \frac{1}{2n} \sum_{i=1}^n (y_i - \beta_0 - x_i \beta')^2 + \lambda P_\alpha(\beta')$$

where  $x_i = (x_{i1}, \dots, x_{ik})$ ,  $\beta' = (\beta_1, \dots, \beta_k)$  for  $1 \leq i \leq n$ ,

$P_\alpha$  is the penalty given by the model (4).

$$(4) \quad P_\alpha(\beta') = (1-\alpha) \frac{1}{2} \|\beta'\|_{L_2}^2 + \alpha \|\beta'\|_{L_1} = \sum_{j=1}^k \left( \frac{1-\alpha}{2} \beta_j^2 + \alpha |\beta_j| \right)$$

As can be seen in equation (4), the penalty factor is a linear combination of norms  $L_1$ ,  $L_2$  and unknown parameters  $\beta'$ . Because of the introduction of a penalty subfunction to the function, which depends on the value of the model parameters (1), the absolute values of these parameters have been reduced. Parameter  $\lambda$  in the task (3) defines the penalty factor, and the parameter  $0 \leq \alpha \leq 1$  creates a compromise between the LASSO (Least Absolute Shrinkage and Selection Operator) regression when  $\alpha = 1$  and pure ridge regression when  $\alpha = 0$ . Ridge regression (called Tikhonov regularization) is one of the first methods of models regularization. LASSO regression was proposed by Robert Tibshirani. It consists in estimating unknown parameters and choosing models.

Solving the task (3) for established  $\lambda$  and  $\alpha$  parameters we calculate estimators of unknown parameters for the model (1) with correlated variables. The expected values of the dependent variables are determined using the equation (5).

$$(5) \quad \hat{Y} = X \hat{\beta}$$

where  $\hat{\beta} = (\hat{\beta}_0, \hat{\beta}_1, \dots, \hat{\beta}_k)$  is an estimator of unknown parameters.

## Results

Fig. 2 shows a spatial model of a part of a flood embankment. All electrodes placed on the surface of the object are on one lane, which is perpendicular to the river bed or the center of the water reservoir. This means that in this case the electrodes were placed across the flood embankment. The tested model had the following parameters:

- type of electrodes: point,
- number of tetrahedrons: 12153,
- number of nodes: 2991,
- number of electrodes: 32.

The carried out experiments included 2 types of current stimulations. The first stimulation contained 192 measurements. The second stimulation contained 96 measurements. Parameters of linear models were generated using the algorithm based on ElasticNET. Fig. 3 shows the results of the obtained reconstructions.

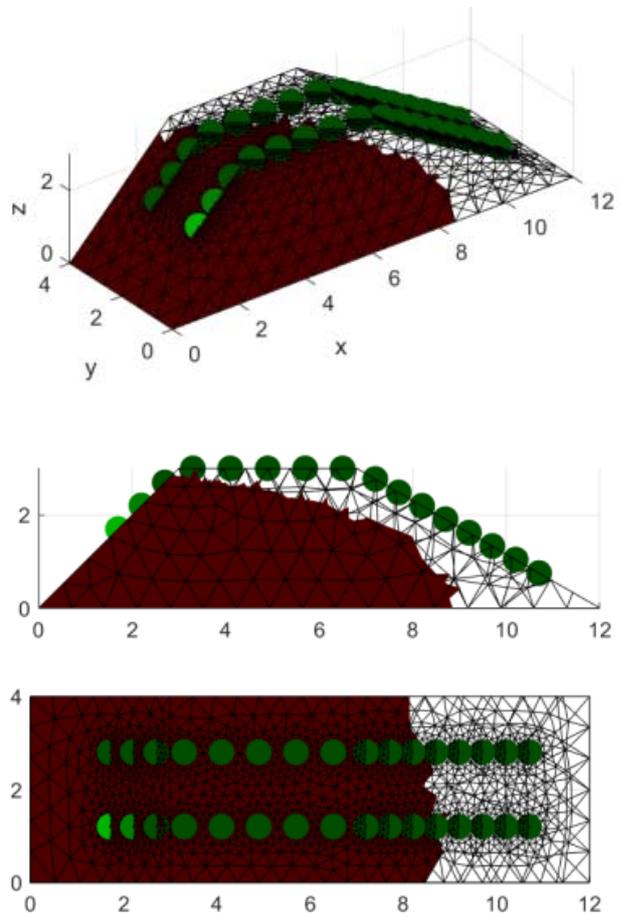
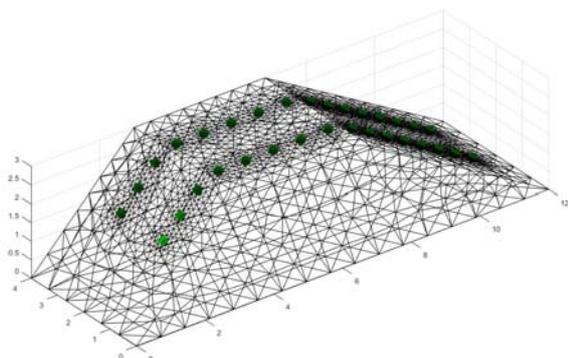


Fig. 2. Model of a flood embankment I with an injection of water.

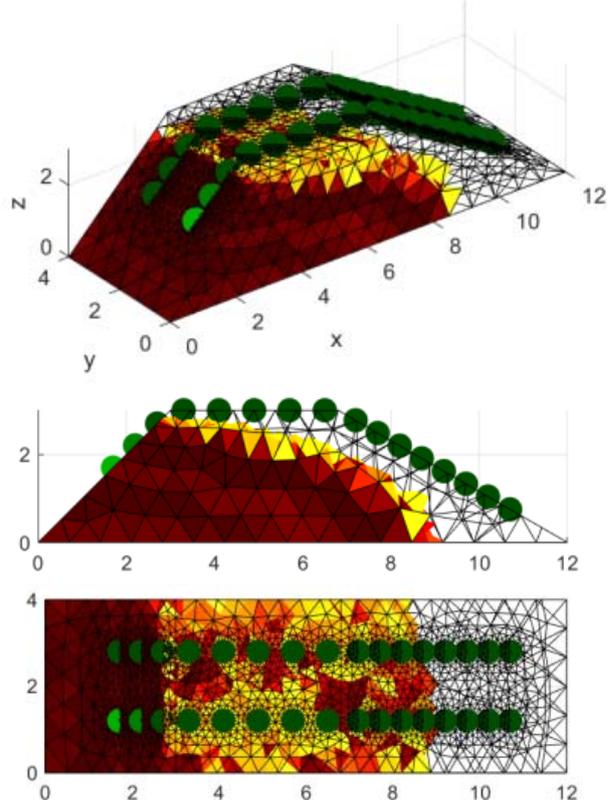


Fig. 3. Image reconstruction by the ElasticNET method.

Fig. 4 shows the three-dimensional model that represents a part of the flood embankment. All electrodes are arranged in two lines, which are parallel to the riverbed

or the shoreline. This means that in this case the electrodes are arranged along the flood embankment or dam.

The tested model had the following parameters:

- type of electrodes: point,
- number of tetrahedrons: 17191,
- number of nodes: 4002,
- number of electrodes: 32.

The carried out experiments included 2 types of current stimulations. The first stimulus contained 192 measurements. The second stimulus contained 96 measurements. Parameters of linear models were estimated using the ElasticNET. Fig. 5 shows the results of the obtained reconstructions.

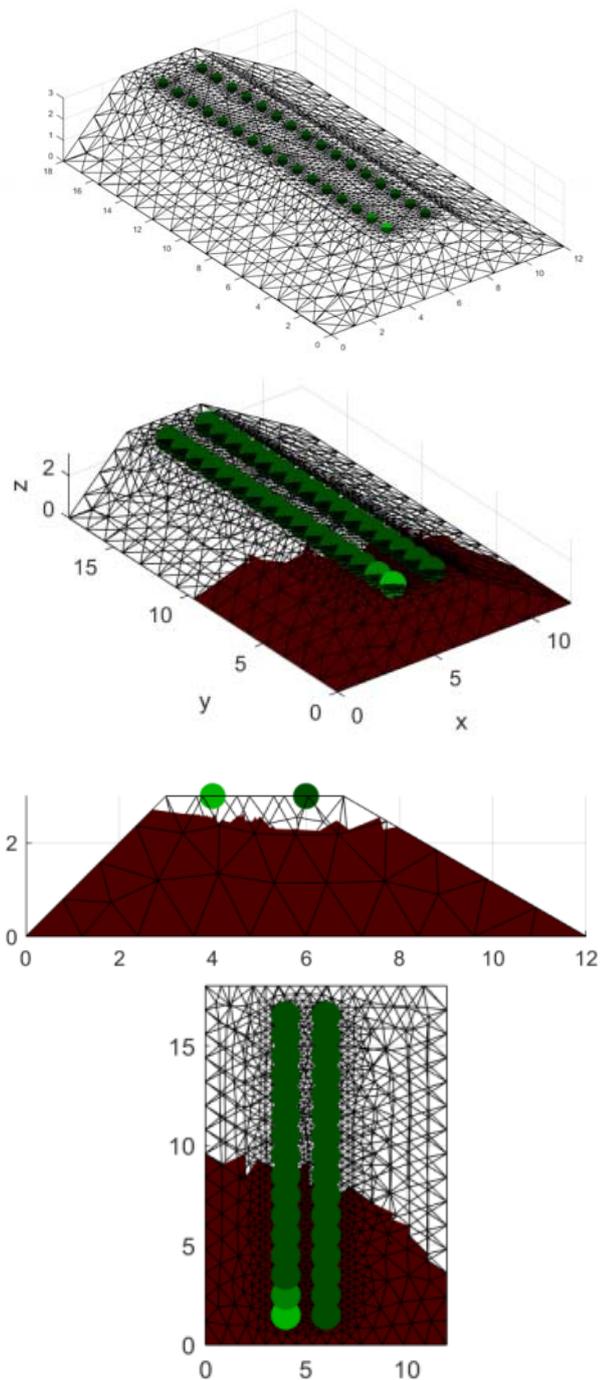


Fig. 4. Model of a flood embankment II with an injection of water.

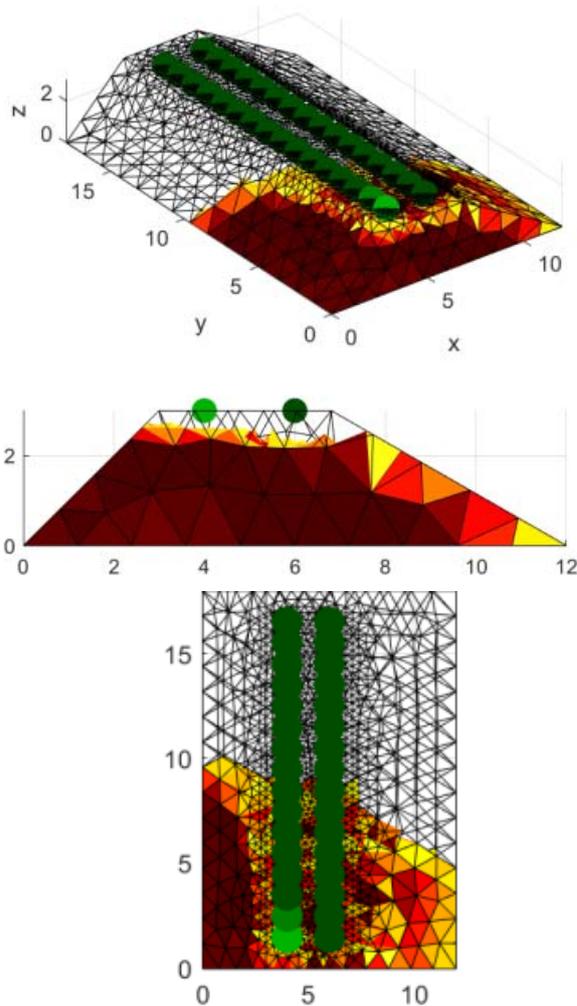


Fig. 5. Analysis of water injection from left side.

## Conclusion

The article proposes an original methodology for solving problems related to risk assessment resulting from damages of flood embankments. The tested algorithm was based on the ElasticNET method. Thanks to the use of ElasticNET it was possible to solve the inverse problem in an efficient and effective manner, which resulted in obtaining more accurate and stable spatial reconstructions of flood embankment cross-sections. The solution developed thanks to the research described above has been successfully used in the embankments and dams simulation models. The results of simulation experiments as well as validations carried out on physical models provided promising results. Future work will be conducted towards the development and implementation of additional statistical algorithms in order to provide the best solution to the inverse problem.

**Authors:** Tomasz Rymarczyk, Ph.D. Eng., University of Economics and Innovation, Projektowa 4, Lublin, Poland / Research & Development Centre Netrix S.A. E-mail: [tomasz@rymarczyk.com](mailto:tomasz@rymarczyk.com); Edward Kozłowski, Ph.D., Lublin University of Technology, Nadbystrzycka 38A, Lublin, Poland, E-mail: [e.kozlowski@pollub.pl](mailto:e.kozlowski@pollub.pl); Przemysław Adamkiewicz, Ph.D., Research & Development Centre Netrix S.A., E-mail: [przemyslaw.adamkiewicz@netrix.com.pl](mailto:przemyslaw.adamkiewicz@netrix.com.pl); Grzegorz Kłosowski, Ph.D. Eng., Lublin University of Technology, Nadbystrzycka 38A, Lublin, Poland, E-mail: [g.klosowski@pollub.pl](mailto:g.klosowski@pollub.pl); Paweł Rymarczyk, Research & Development Centre Netrix S.A., E-mail: [pawel.rymarczyk@netrix.com.pl](mailto:pawel.rymarczyk@netrix.com.pl); Jan Sikora, Professor, Eng., Research & Development Centre Netrix S.A., E-mail: [j.sikora@pollub.pl](mailto:j.sikora@pollub.pl).

## REFERENCES

- [1] Rymarczyk T., Kozłowski E., Kłosowski G., Paweł Rymarczyk, Adamkiewicz and Sikora J., Elastic net method in the image reconstruction infiltration of water in the embankment, *PTZE — 2018 Applications of Electromagnetic in Modern Techniques and Medicine*, 09-12 September 2018, Raclawice, Poland.
- [2] Allaire G., De Gournay F., Jouve F., and Toader A. M., Structural optimization using topological and shape sensitivity via a level set method, *Control and Cybernetics*, 34 (2005), 59–80.
- [3] Babout L., Grudzień K., Wiącek J., Niedostatkiwicz M., Karpiński B., Szkodo M., „Selection of material for X-ray tomography analysis and DEM simulations: comparison between granular materials of biological and non-biological origins, *Granular Matter*, 20 (2018), No. 3, 20:38.
- [4] Bartušek K.; Fiala P., Mikulka J., Numerical Modeling of Magnetic Field Deformation as Related to Susceptibility Measured with an MR System, *Radioengineering*, 17 (2008), No. 4, 113-118.
- [5] Bartusek K., Kubasek R., Fiala P., Determination of pre-emphasis constants for eddy current reduction, *Measurement science and technology*, 21 (2010), No. 10, 105601.
- [6] Beck M. S., Byars M., Dyakowski T., Waterfall R., He R., Wang S. J., Yang W. Q., Principles and Industrial Applications of Electrical Capacitance Tomography, *Measurement and Control*, September, 30, 7 (1997).
- [7] Borcea L., Electrical impedance tomography, *Inverse Problems*, 18 (2002), 99–136.
- [8] Borsoi R. A., Aya J. C. C., Costa G. H., and Bermudez J. C. M., Super-resolution reconstruction of electrical impedance tomography images,” *Comput. Electr. Eng.*, 69 (2018), 1–13.
- [9] Celik N., Manivannan N., Strudwick A., and Balachandran W., Graphene-enabled electrodes for electrocardiogram monitoring, *Nanomaterials*, 6 (2016), No. 9, [Online]. Available: <http://www.mdpi.com/2079-4991/6/9/156>
- [10] Grudzien, K., Chaniecki, Z., Romanowski, A., Sankowski, D., Nowakowski, J., & Niedostatkiwicz, M. (2016, May). Application of twin-plane ECT sensor for identification of the internal imperfections inside concrete beams. In *Instrumentation and Measurement Technology Conference Proceedings (I2MTC)*, (2016) IEEE International, 1-6.
- [11] Chen C., Woźniak P., Romanowski A. et al., Using Crowdsourcing for Scientific Analysis of Industrial Tomographic Images, *ACM Transactions on Intelligent Systems and Technology*, 7 (2016), No. 4, 52:1–52:25.
- [12] De Donno G., Di Giambattista L., Orlando L., High-resolution investigation of masonry samples through GPR and electrical resistivity tomography. *Construction and Building Materials*, 154, (2017), 1234-1249.
- [13] Duda K., Adamkiewicz A., Rymarczyk T., Nondestructive Method to Examine Brick Wall Dampness, *International Interdisciplinary Phd Workshop 2016*, (2016), 68-71.
- [14] Fiala P., Drexler P., Nešpor D., Szabó Z., Mikulka J., Polívka J., The Evaluation of Noise Spectroscopy Tests, *ENTROPY*, 18 (2016), No. 12, 1-16.
- [15] Filipowicz S.F., Rymarczyk T., Measurement Methods and Image Reconstruction in Electrical Impedance Tomography, *Przegląd Elektrotechniczny*, 88 (2012), No. 6, 247-250.
- [16] Kłosowski G., Kozłowski E., Gola A., Integer linear programming in optimization of waste after cutting in the furniture manufacturing, *Advances in Intelligent Systems and Computing 2018*; 637 (2018), 260-270.
- [17] Kosicka E., Kozłowski E., and Mazurkiewicz D., Intelligent Systems of Forecasting the Failure of Machinery Park and Supporting Fulfilment of Orders of Spare Parts, (2018), 54–63.
- [18] Kryszyn J., Radzik B., Olszewski T., Szabatin R., Smolik W., Single-shot high-voltage circuit for electrical capacitance tomography, *Measurement Science and Technology*, 28 (2017), No.2, 025902.
- [19] Krawczyk A., Korzeniewska E., Łada-Tondyrya E., Magnetophosphenes – History and contemporary implications”, *Przegląd Elektrotechniczny*, 94 (2018), No. 1, 61-64.
- [20] Korzeniewska E., Walczak M., Rymaszewski J., Elements of Elastic Electronics Created on Textile Substrate, *Proceedings of the 24th International Conference Mixed Design of Integrated Circuits and Systems - MIXDES 2017*, 2017, 447-45.
- [21] Lopato P., Chady T., Sikora R., Ziolkowski S., M., Full wave numerical modelling of terahertz systems for nondestructive evaluation of dielectric structures, 32 (2013), No. 3, 736 – 749.
- [22] Majchrowicz M., Kapusta P., Jackowska-Strumiłło L., Sankowski D., Optimization of Distributed Multi-node, Multi-GPU, Heterogeneous System for 3D Image Reconstruction in Electrical Capacitance Tomography, *Image processing & communications*, 21 (2016), No. 3, 81-90.
- [23] Majchrowicz M., Kapusta P., Jackowska-Strumiłło L., Sankowski D., Acceleration of image reconstruction process in the electrical capacitance tomography 3d in heterogeneous, multi-gpu system, *Informatyka, Automatyka, Pomiary w Gospodarce i Ochronie Środowiska (IAPGOŚ)*, 7 (2017), No. 1, 37-41; DOI: 10.5604/01.3001.0010.4579
- [24] Polakowski K., Filipowicz S.F., Sikora J., Rymarczyk T., Tomography technology application, *Przegląd Elektrotechniczny*, 84 (2008), No. 12, 227-229.
- [25] Psuj G., “Multi-Sensor Data Integration Using Deep Learning for Characterization of Defects in Steel Elements, *Sensors*, 18 (2018), No. 1, 292; <https://doi.org/10.3390/s18010292>
- [26] Romanowski A., Big Data-Driven Contextual Processing Methods for Electrical Capacitance Tomography, *IEEE Transactions on Industrial Informatics*, (2018), 1551-3203, DOI: 10.1109/TII.2018.2855200
- [27] Rymarczyk T., Sikora J., Applying industrial tomography to control and optimization flow systems, *Open Physics*, 16 (2018); 332–345, DOI: <https://doi.org/10.1515/phys-2018-0046>
- [28] Rymarczyk T., Kłosowski G., Application of neural reconstruction of tomographic images in the problem of reliability of flood protection facilities, *Eksploatacja i Niezawodność – Maintenance and Reliability* 20 (2018), No. 3, 425–434 <http://dx.doi.org/10.17531/ein.2018.3.11>
- [29] Rymarczyk T., Kłosowski G., Kozłowski E., Non-Destructive System Based on Electrical Tomography and Machine Learning to Analyze Moisture of Buildings, *Sensors*, 18 (2018), No.7, 2285.
- [30] Soleimani M., Mitchell C.,N., Banasiak R., Wajman R., Adler A., Four-dimensional electrical capacitance tomography imaging using experimental data, *Progress In Electromagnetics Research*, 90 (2009), 171-186.
- [31] Smolik W., Kryszyn J., Olszewski T., Szabatin R., Methods of small capacitance measurement in electrical capacitance tomography, *Informatyka, Automatyka, Pomiary w Gospodarce i Ochronie Środowiska (IAPGOŚ)*, 7 (2017), No. 1, 105-110; DOI: 10.5604/01.3001.0010.4596
- [32] Wajman R., Fiderek P., Fidos H., Sankowski D., Banasiak R., Metrological evaluation of a 3D electrical capacitance tomography measurement system for two-phase flow fraction determination, *Measurement Science and Technology*, 24 (2013), No. 6, 065302.
- [33] Ziolkowski M., Gratkowski S., and Zywicka A. R., Analytical and numerical models of the magnetoacoustic tomography with magnetic induction,” *COMPEL - Int. J. Comput. Math. Electr. Electron. Eng.*, 37 (2018), No. 2, 538–548.